

Problema 1 Sean $z_1 = 2 + i$ y $z_2 = -1 + 2i$. Calcular: $z_1 + z_2$, $z_1 \cdot z_2$ y $\frac{z_1}{z_2}$.

Solución:

- $z_1 + z_2 = 1 + 3i$
- $z_1 \cdot z_2 = -4 + 3i$
- $\frac{z_1}{z_2} = -i$

Problema 2 Resolver la ecuación $z^4 + 1 - i = 0$

Solución:

$$z^4 + 1 - i = 0 \implies z = \sqrt[4]{-1 + i} = \sqrt[8]{(2)_{135^\circ}} =$$

$$\left\{ \begin{array}{l} \sqrt[8]{2} \frac{135^\circ + 0^\circ}{4} = \sqrt[8]{2}(\cos 33^\circ 45' + i \sin 33^\circ 45') \\ \sqrt[8]{2} \frac{135^\circ + 360^\circ}{4} = \sqrt[8]{2}(\cos 123^\circ 45' + i \sin 123^\circ 45') \\ \sqrt[8]{2} \frac{135^\circ + 720^\circ}{4} = \sqrt[8]{2}(\cos 213^\circ 45' + i \sin 213^\circ 45') \\ \sqrt[8]{2} \frac{135^\circ + 1080^\circ}{4} = \sqrt[8]{2}(\cos 303^\circ 45' + i \sin 303^\circ 45') \end{array} \right.$$